

# **Gravitation Astrometric Measurement Experiment (GAME)**

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3) ALTEC

4) Politecnico di Torino

# GAME:

Gravitation → PPN parameters  $\gamma$  and  $\beta$

Astrometric → Apparent star position variation

Measurement → Light deflection  
close to the Sun

Experiment → Space mission – small / medium

## Approach:

build on flight inheritance from past missions

[SOHO, STEREO, Hipparcos, **Gaia**]

# GAME Science goals

## \* Characterisation of weak field gravity in the Solar System:

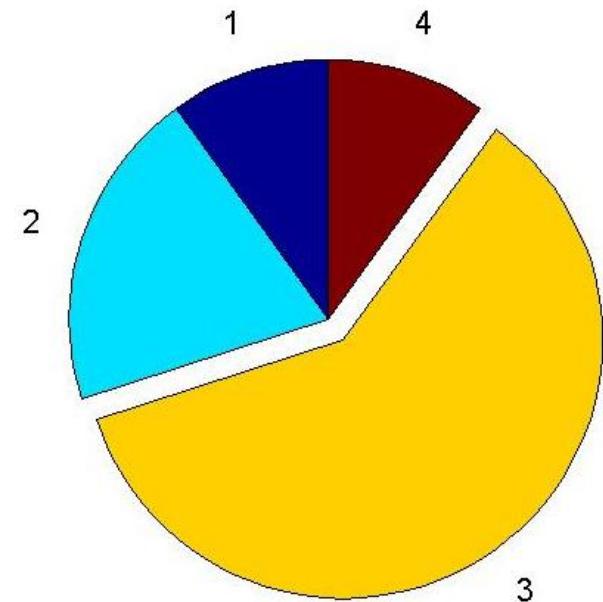
- Parametrised Post-Newtonian parameters  $\gamma, \beta$
- Relativistic effects of oblate and moving giant planets
- High precision ephemerides of major planets

## \* Science bonus:

- Extra-solar Planetary systems
- Stellar astrophysics
- Upper limits on some Lorentz-violating SME parameters

# GAME vs. ESA Cosmic Vision “Grand Themes”

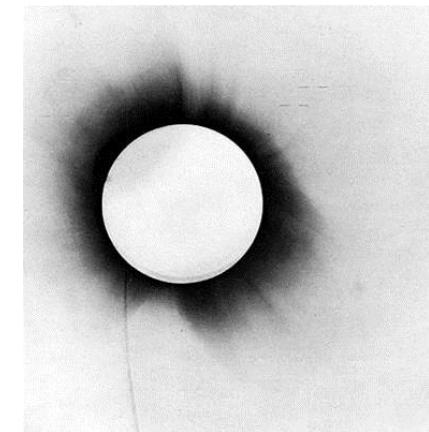
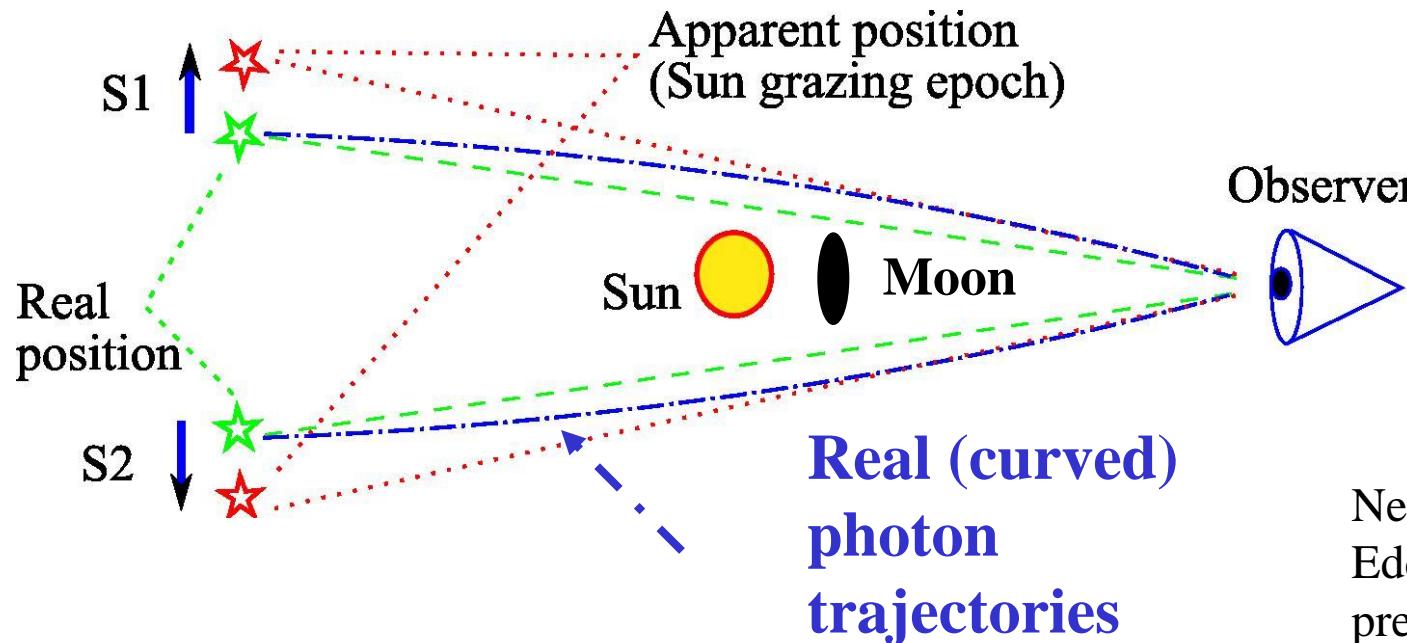
	Cosmic Vision Theme	GAME
1	What are the conditions for planet formation and the emergence of life?	10%
2	How does the Solar System work?	20%
3	<b>What are the fundamental physical laws of the Universe?</b>	<b>60%</b>
4	How did the Universe originate and what is it made of?	10%



Main science case:

**Astrometric tests of General Relativity in Solar system**

# Dyson-Eddington-Davidson experiment (1919) - I



Negative sample from  
Eddington's photographs,  
presented in 1920 paper

First test of General Relativity by light deflection nearby the Sun

**Epoch (a):** unperturbed direction of stars S1, S2 (dashed lines)

**Epoch (b):** apparent direction as seen by observer (dotted line)

# Dyson-Eddington-Davidson experiment (1919) - II

Repeated throughout  
XX century

Precision achieved:  
~10%

[A. Vecchiato et al., MGM 11 2006]

**Limiting factors:**

- **Need for natural eclipses** → Short exposures, high background
- **Atmospheric turbulence** → Large astrometric noise
- **Portable instruments** → Limited resolution, collecting area

Authors	Year	Deflection ["]
Dyson & al.	1920	$1.98 \pm 0.16$
Dodwell & al.	1922	$1.77 \pm 0.40$
Freundlich & al.	1929	$2.24 \pm 0.10$
Mikhailov	1936	$2.73 \pm 0.31$
van Biesbroeck	1947	$2.01 \pm 0.27$
van Biesbroeck	1952	$1.70 \pm 0.10$
Schmeidler	1959	$2.17 \pm 0.34$
Schmeidler	1961	$1.98 \pm 0.46$
TMET	1973	$1.66 \pm 0.19$

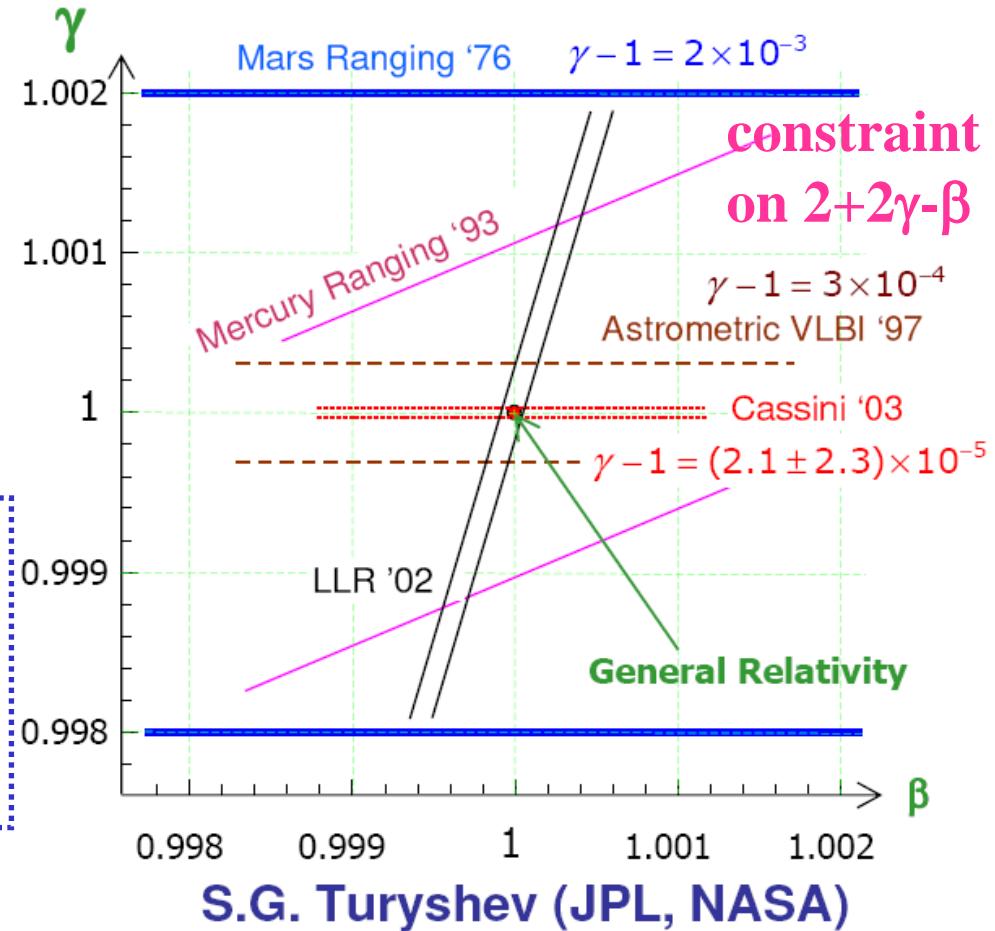
# Why testing GR through $\gamma$ (+ $\beta$ )?

Current experimental bounds:  
consistent with GR

$$|\gamma - 1| \leq 2 \times 10^{-5}$$

$$|\beta - 1| \leq 1 \times 10^{-4}$$

Parametrised Post-Newtonian  
(PPN) formulation allows  
comparison of competing  
gravitation theories



Deviation range expected:

$$10^{-5} - 10^{-7}$$

*Living Reviews in Relativity*, C.F. Will (2001)

# Cosmological implications

- Dark Matter and Dark Energy: explain experimental data
- Alternative explanations: modified gravity theories – e.g.  $f(R)$
- Possible check: fit of gravitation theories with observations
- Check of modified gravitation theories within Solar System

## Rationale:

replacement in Einstein's field equations of  
**source terms** [ $\Leftrightarrow$  **new particles**] on one side with  
**geometry terms** [ $\Leftrightarrow$  **intrinsic curvature**] on the other side

# *DE and DM from the Observations*

- Universe evolution is characterized by different phases of expansion

*Dark Matter*

*Ordinary Matter*

*Radiation*

ACS  
discovers  
two distant  
Type Ia  
supernovae

Farthest  
supernova

Deceleration

Acceleration

Big Bang

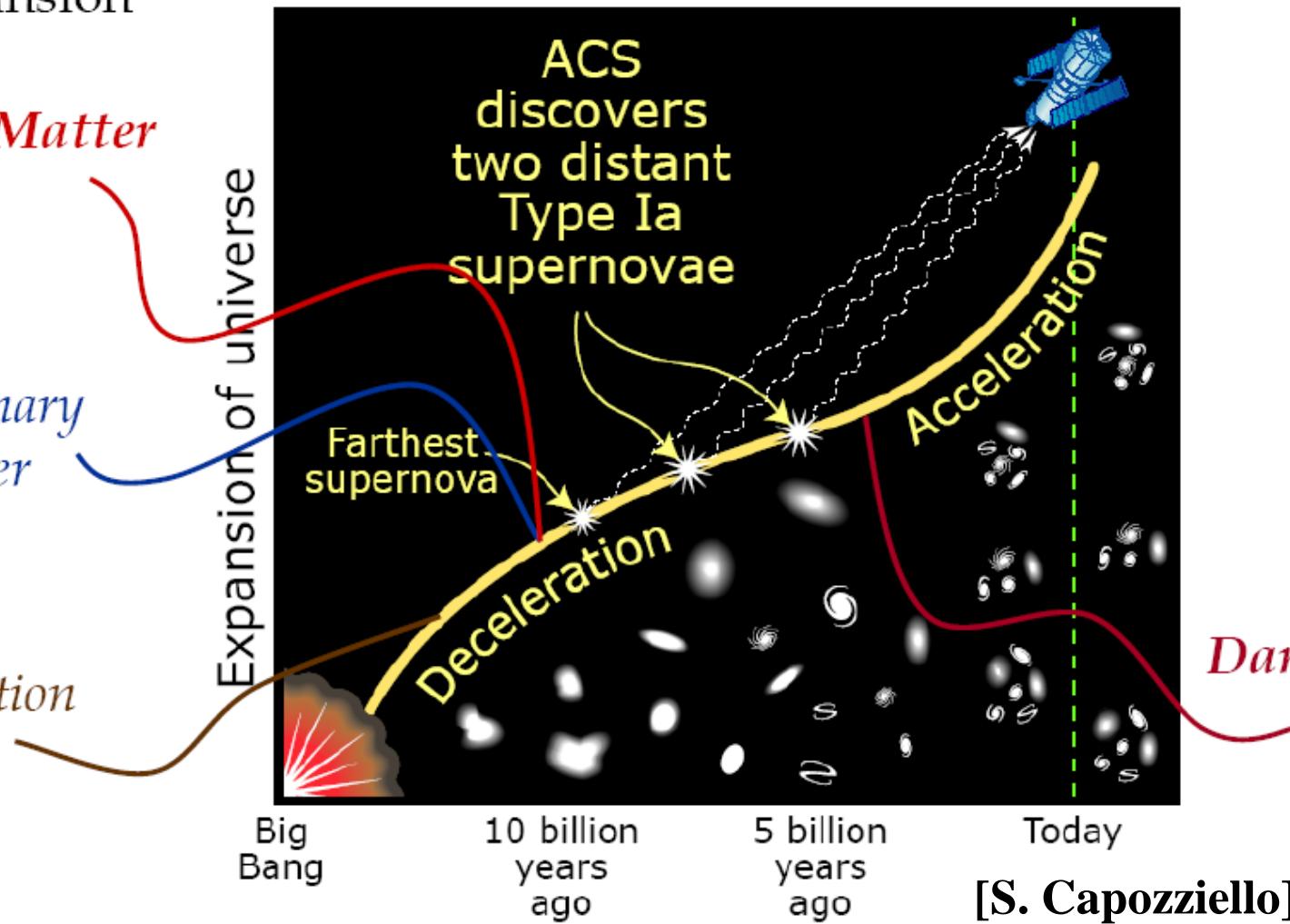
10 billion  
years ago

5 billion  
years ago

Today

[S. Capozziello]

*Dark Energy*



# Constraining the phase space of modified gravity

Taking advantage of PPN limit, e.g. for  $f(R)$  theories...

$$\gamma_R^{PPN} - 1 = \frac{-f''(R)^2}{f'(R) + 2f''(R)^2}, \quad \beta_R^{PPN} - 1 = \frac{1}{4} \left[ \frac{f'(R) \cdot f''(R)}{2f'(R) + 3f''(R)^2} \cdot \frac{d\gamma_R^{PPN}}{d\phi} \right]$$

[Capozziello & Troisi 2005]

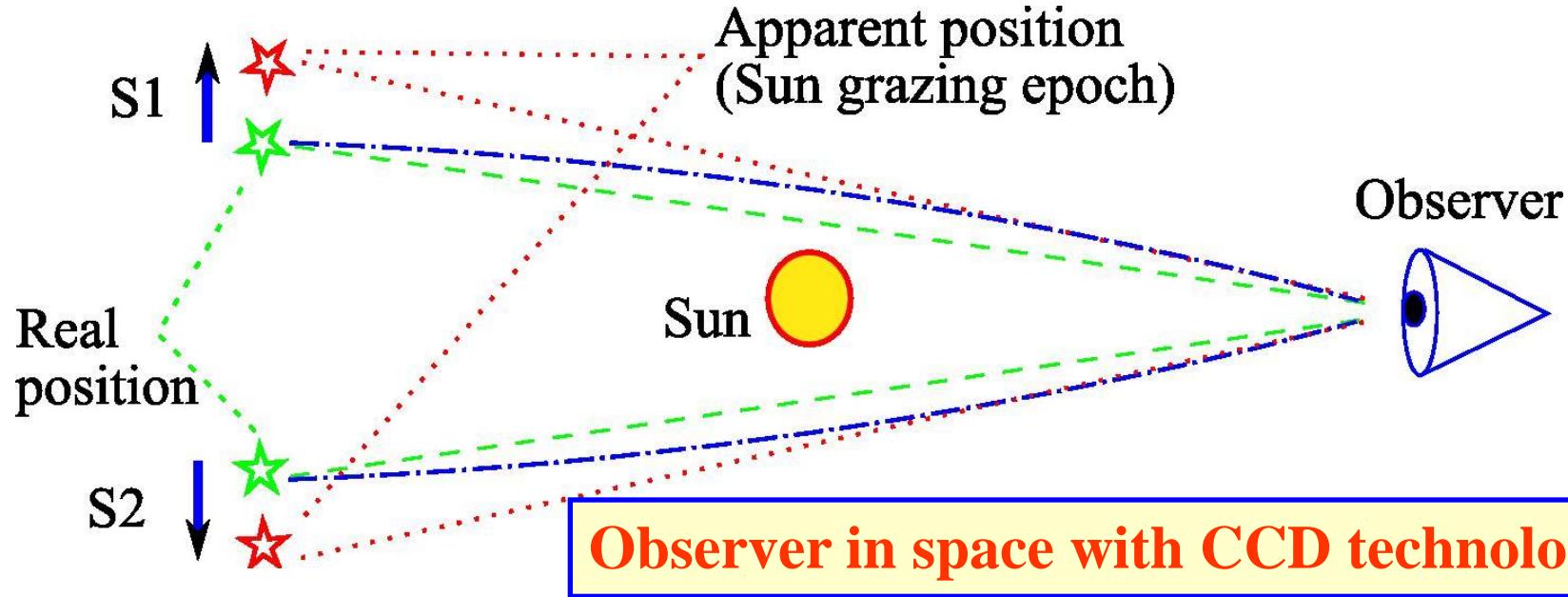
Alternative formulation:

$$\gamma_R^{PPN} - 1 = \frac{-\left(f'' \frac{dR}{d\phi}\right)^2}{Zf' + 2\left(f'' \frac{dR}{d\phi}\right)^2}, \quad \beta_R^{PPN} - 1 = \frac{1}{4} \left[ \frac{f' \cdot f'' \frac{dR}{d\phi}}{2Zf' + 3\left(f'' \frac{dR}{d\phi}\right)^2} \cdot \frac{d\gamma}{dR} \cdot \frac{dR}{d\phi} \right]$$

[Capone & Ruggiero 2010]

**Check of gravitation theories within Solar System:  
local measurements  $\Rightarrow$  cosmological constraints**

# The GAME concept (I)

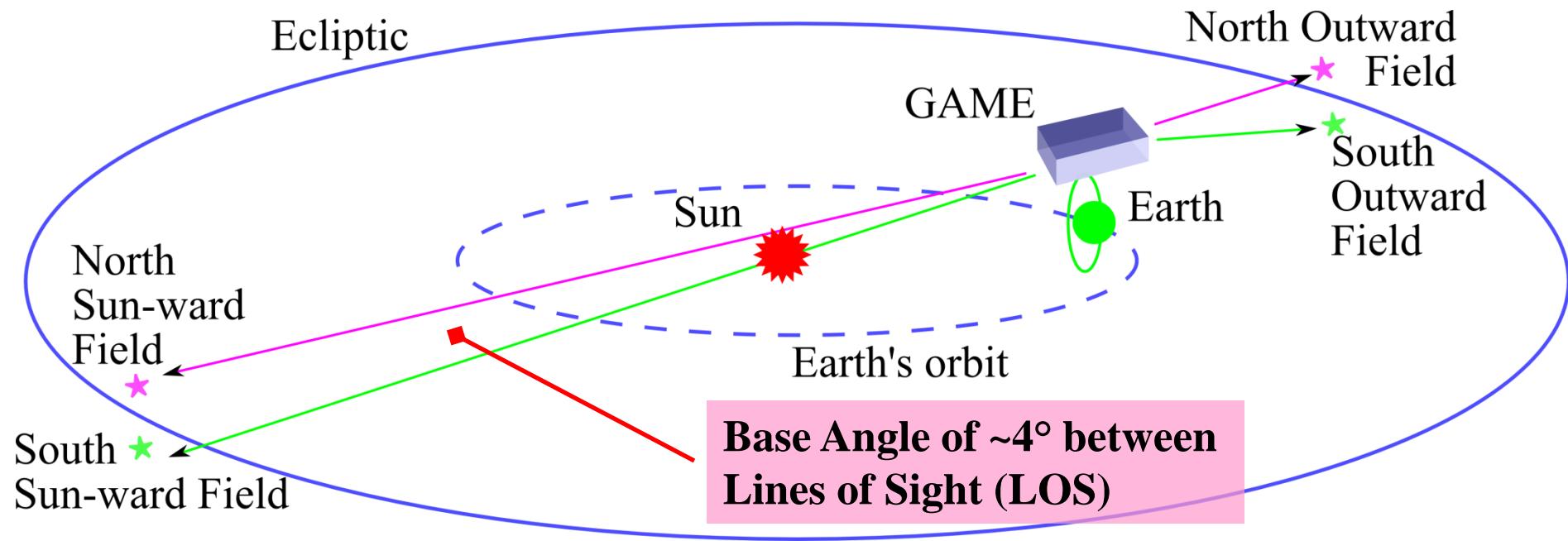


A space mission in the visible range to achieve

- long permanent artificial eclipses
- no atmospheric disturbances, low noise

Differential measurement for systematic error control

# The GAME concept (II)



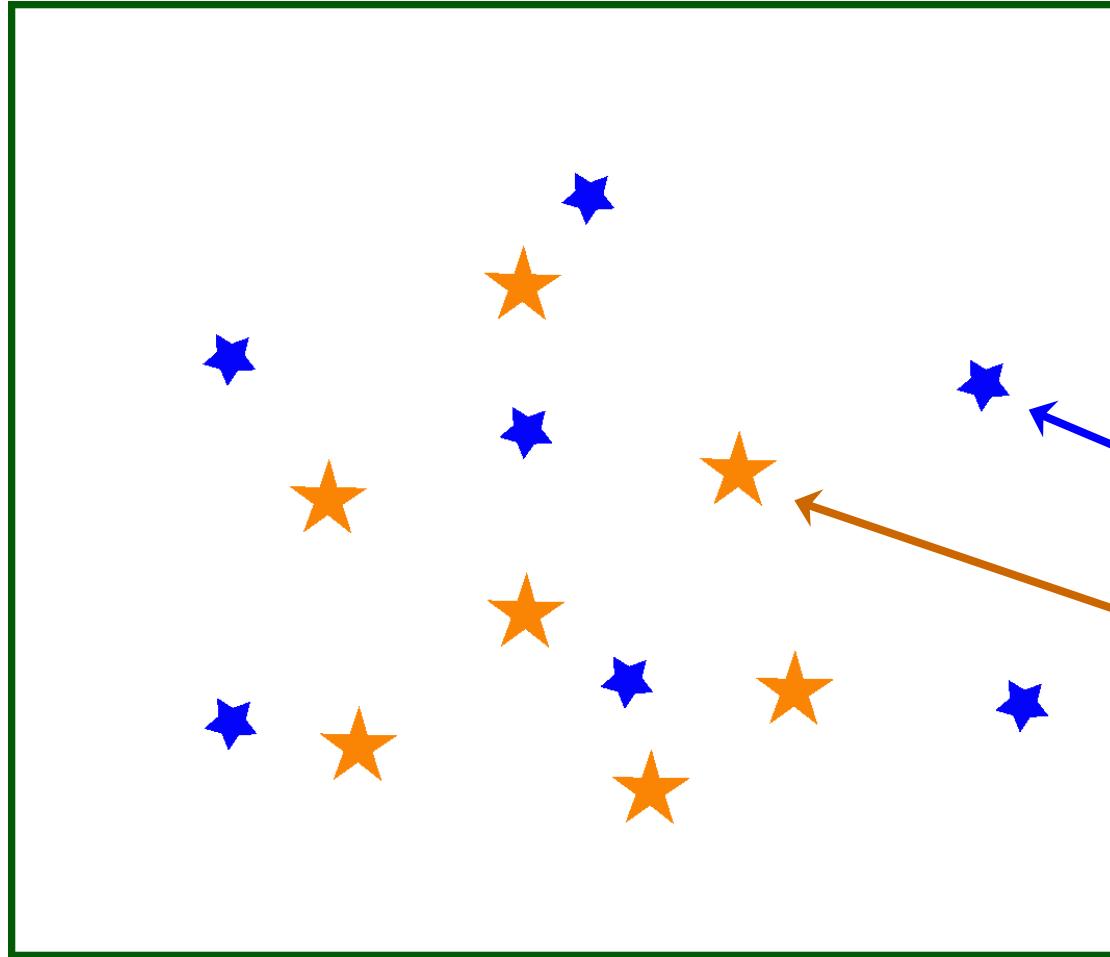
**Experimental approach:**

**Repeated observation of fields close to the Ecliptic**

**Measurement of angular separation of stars between fields**

**2+ epochs to modulate deflection (Sun gravity “switched” on/off)**

# Dual field superposition + epoch modulation



Two epochs:  
differential measure-  
ment of deflection

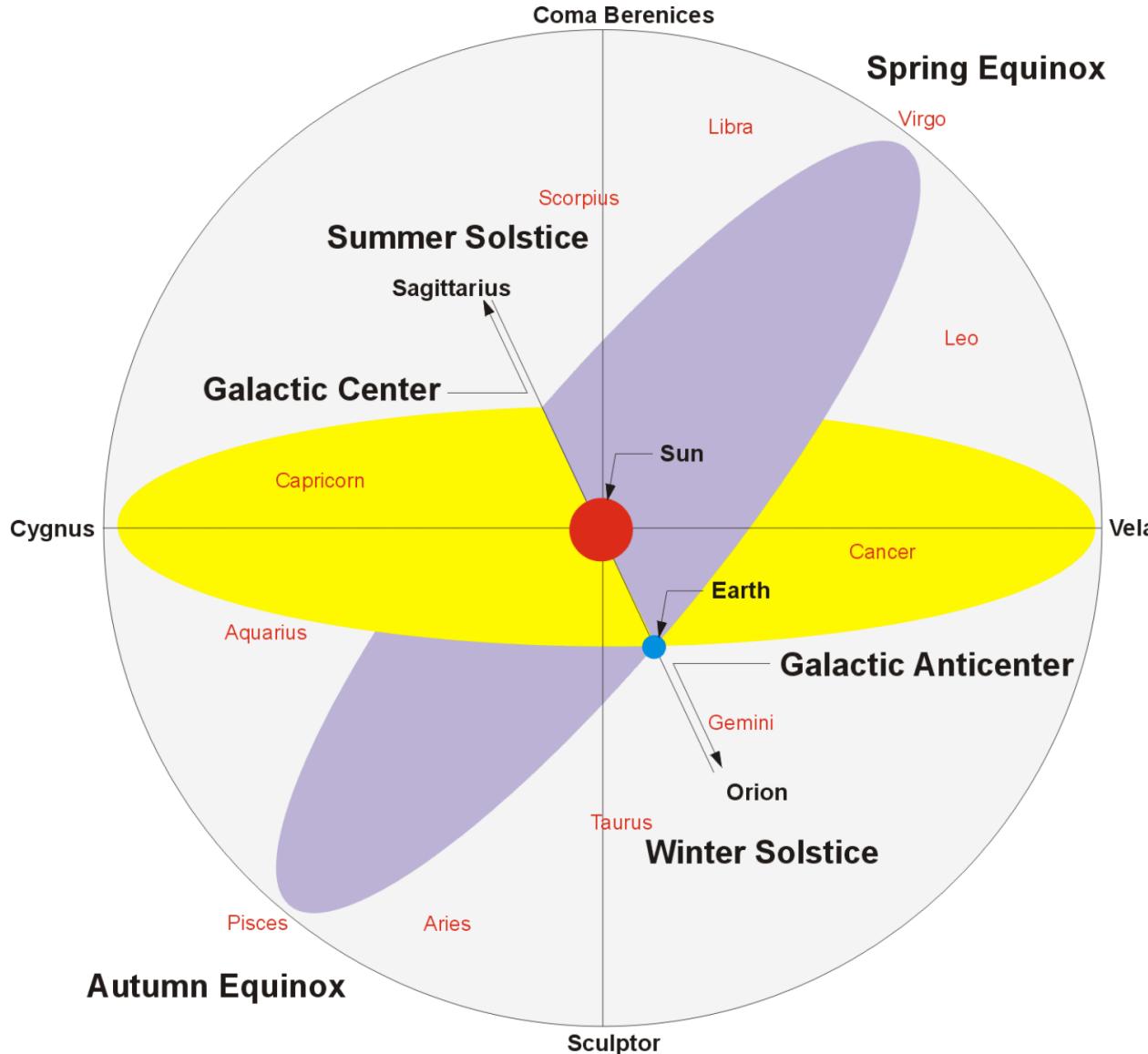
Pointing set on one field

Apparent common  
mode displacement of  
stars in other field

Instrument errors  
mostly common mode

Gaia catalogue: unperturbed positions, proper motions, multiplicity, colour

# Convenient fields: Galactic $\cap$ Ecliptic plane



**High stellar density regions:**

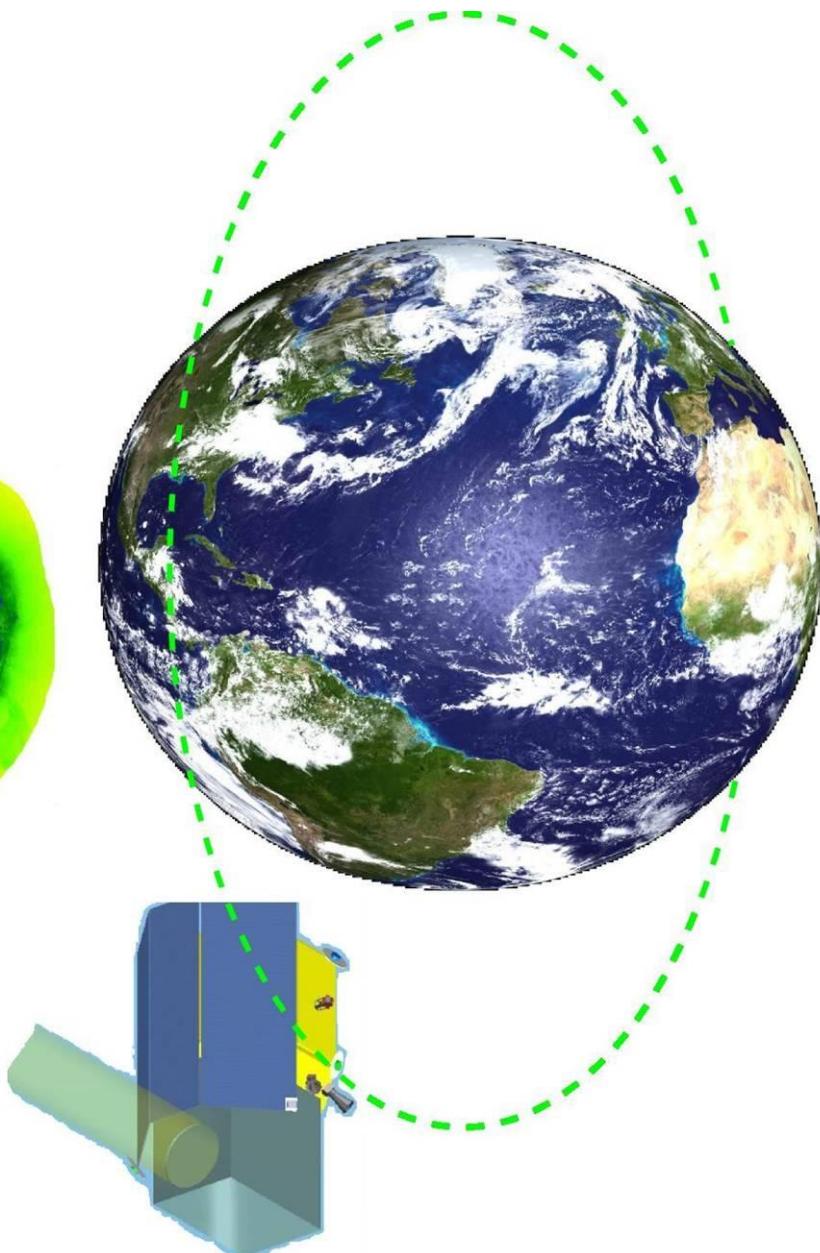
intersection of  
Galactic and  
Ecliptic planes,  
toward Galactic  
centre / anti-centre

# Mission profile

Sun-synchronous orbit,  
1500 km elevation  $\Rightarrow$   
no eclipse

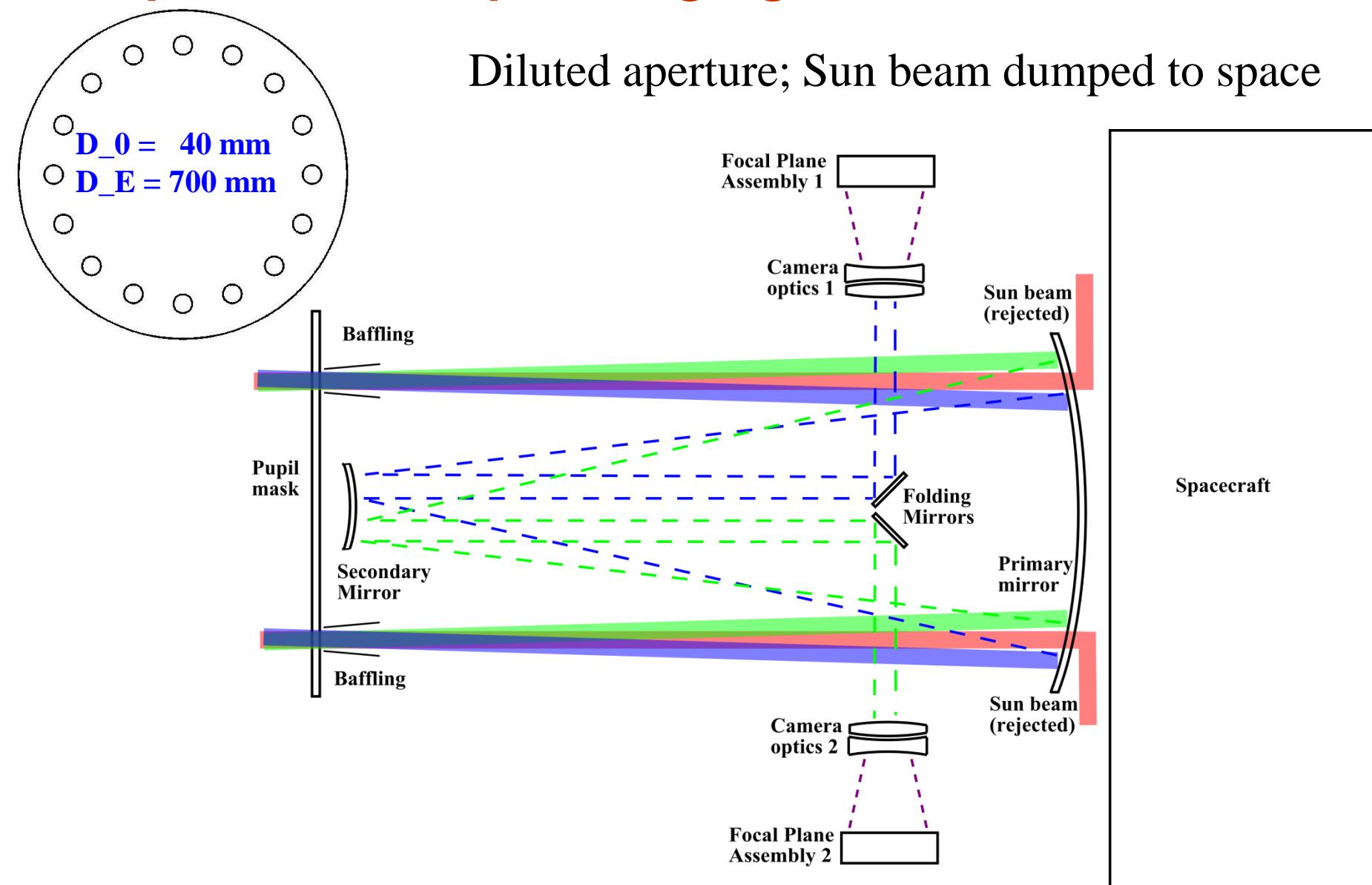
100% nominal  
observing time

Stable solar power  
supply and thermal  
environment  $\Rightarrow$   
instrument structural  
stability



# Payload concept: imaging Fizeau interferometer

Diluted aperture; Sun beam dumped to space



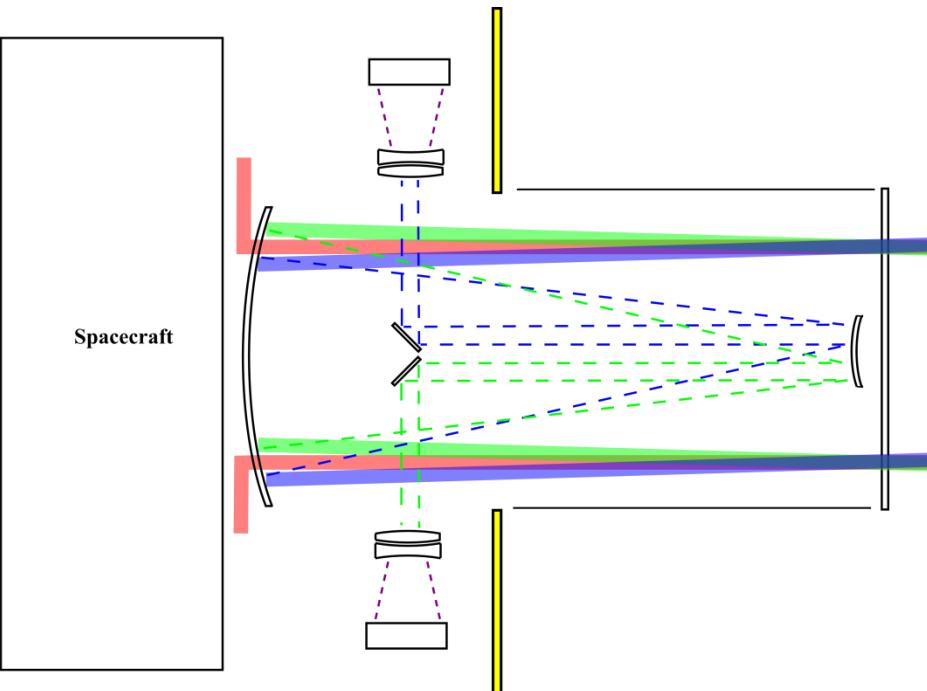
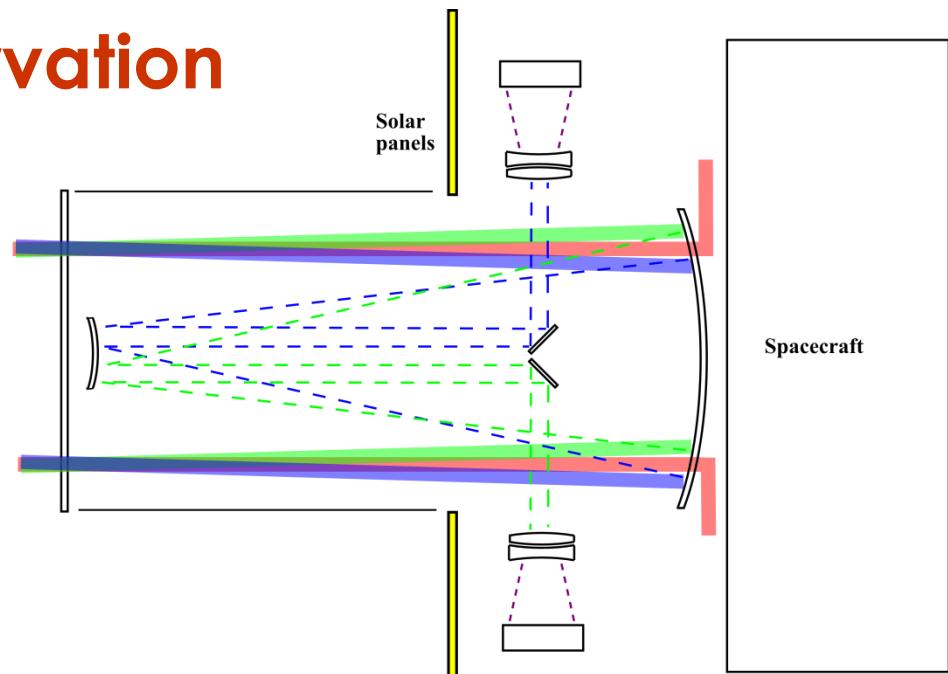
# Observation

On deflected fields

Attitude options:

- Point on Sun
- Scan around Sun

Field 1  
★  
Sun  
Field 2



# Calibration

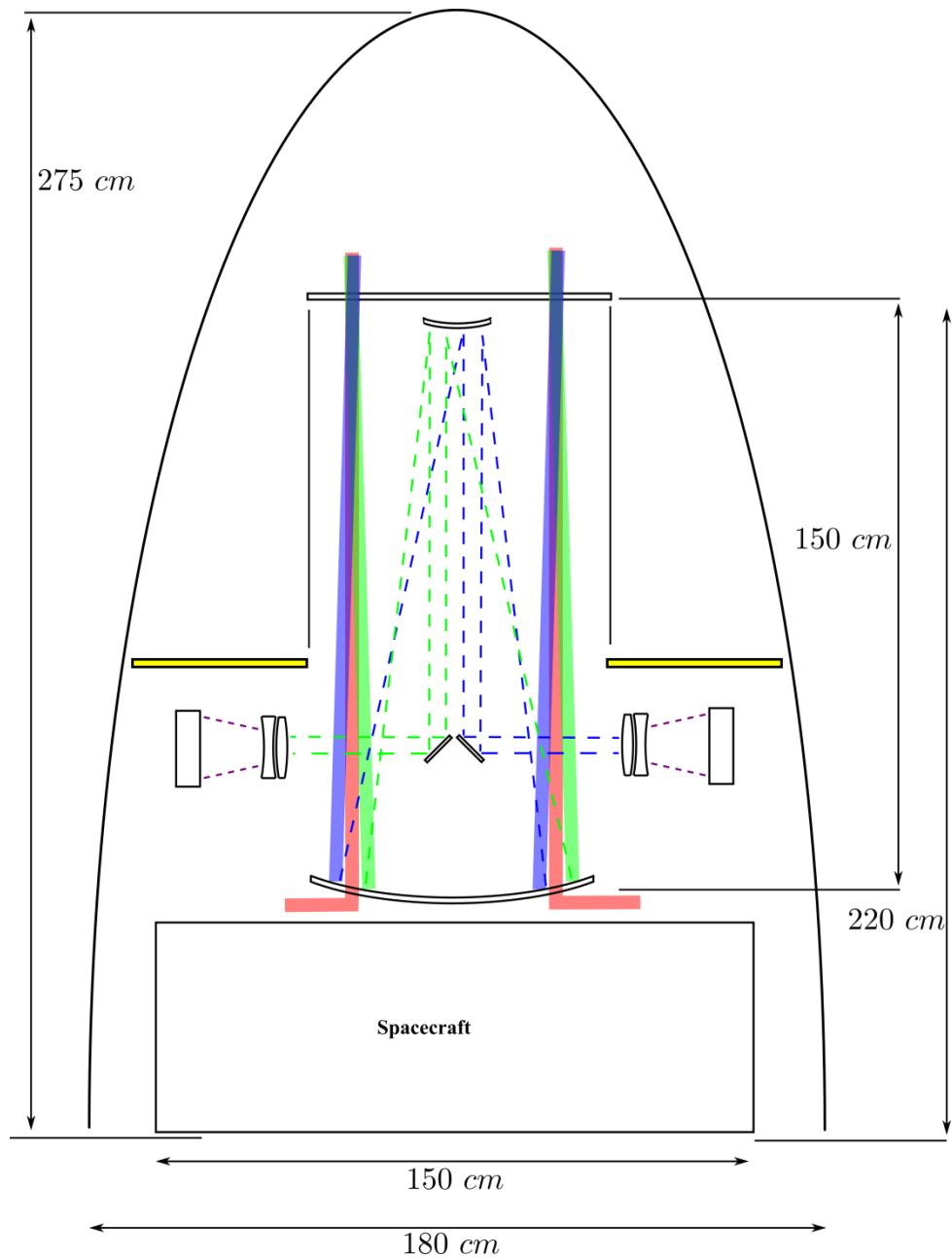
- On undeflected fields
- Periodic anti-Sun pointing

# Fairing volume usage

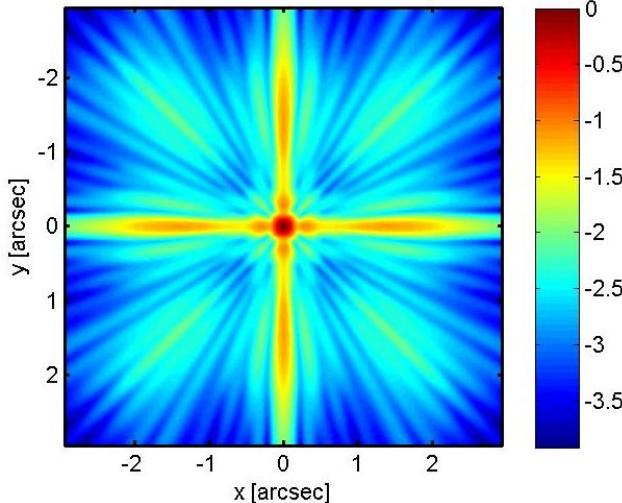
Spacecraft + payload length: 2.2 m  
(without interface)

No deployable subsystems

Compatible with small additional payloads



# Individual imaging and location performance

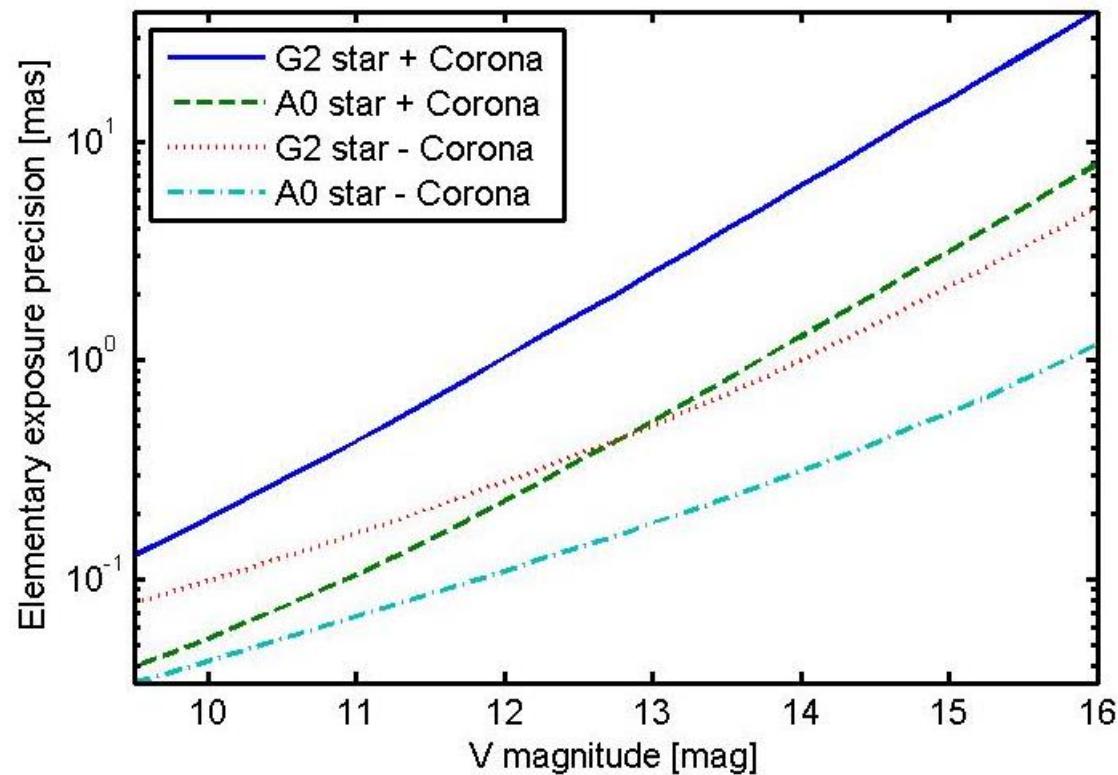


Near-solar unresolved star  
[log intensity]

High resolution images: ~0.2 arcsec peak

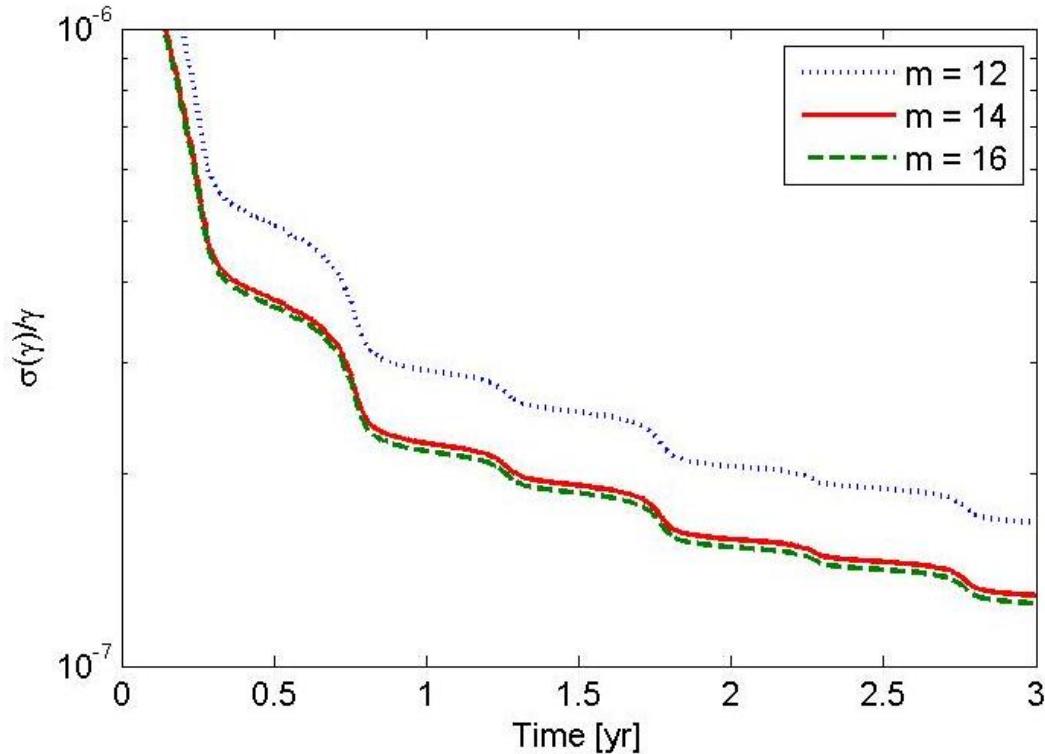
Underlying structure: spoiler detection

Photometry on side wings at <1%



Elementary precision on  
location in 5 min. integration

# Photon limited performance – full mission



$$\frac{\sigma(\gamma)}{\gamma} < 2 \times 10^{-7}$$

$$\frac{\sigma(\beta)}{\beta} < 1 \times 10^{-5}$$

in 2 years

3 year mission extension: improve on calibration and other science topics

Medium class mission:  $\sim 10\times$  performance improvement on  $\gamma$  and  $\beta$

# Laboratory prototype - I

## Diluted SiC Mirror Demonstrator

Pupil mask [shading the telescope]

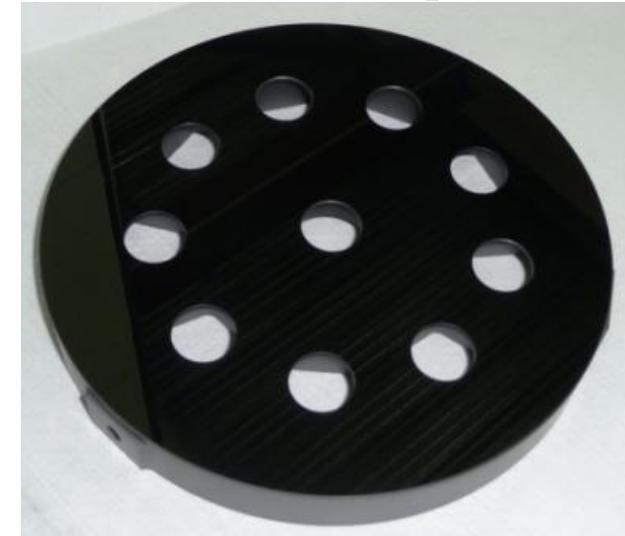
9+1 apertures,  $\varnothing$  20 mm

Outer diameter: 20 cm

Manufacturer: **Boostec** (Bazet, F)

Qualification tests at ADS Intl. (LC)

[photo]



**Requirements:**  
Static & dynamic  
load compatible with  
e.g. Soyuz launcher



# Laboratory prototype - II

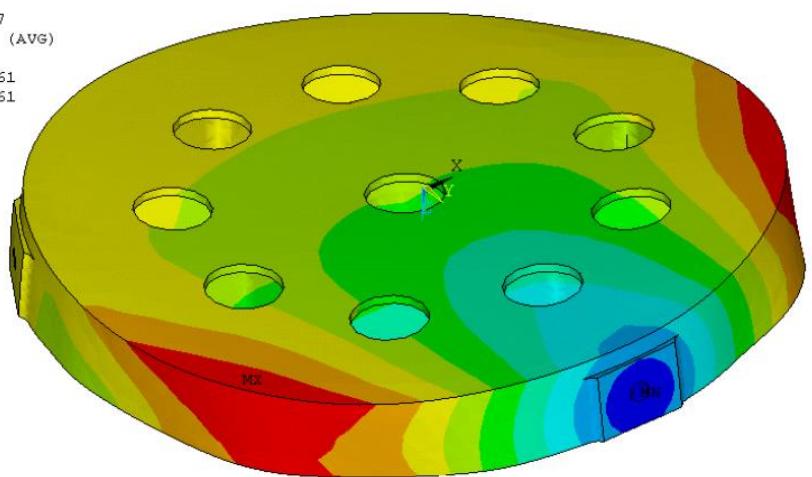
Dynamic analysis (example)

3 clamping areas

First mode: 2817 Hz

1 NODAL SOLUTION

STEP=1  
SUB =1  
FREQ=2817  
USUM (AVG)  
RSYS=0  
DMX =1.961  
SMX =1.961

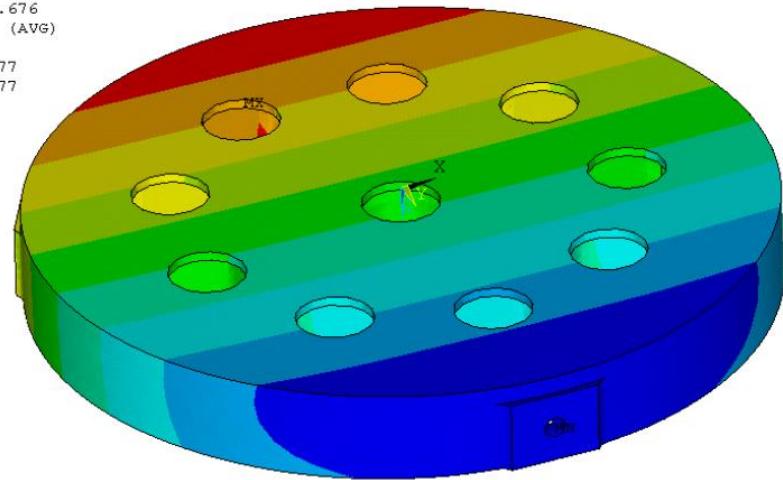


ANSYS

JUN 15 2012  
14:26:41

1 NODAL SOLUTION

STEP=1  
SUB =1  
FREQ=197.676  
USUM (AVG)  
RSYS=0  
DMX =2.277  
SMX =2.277

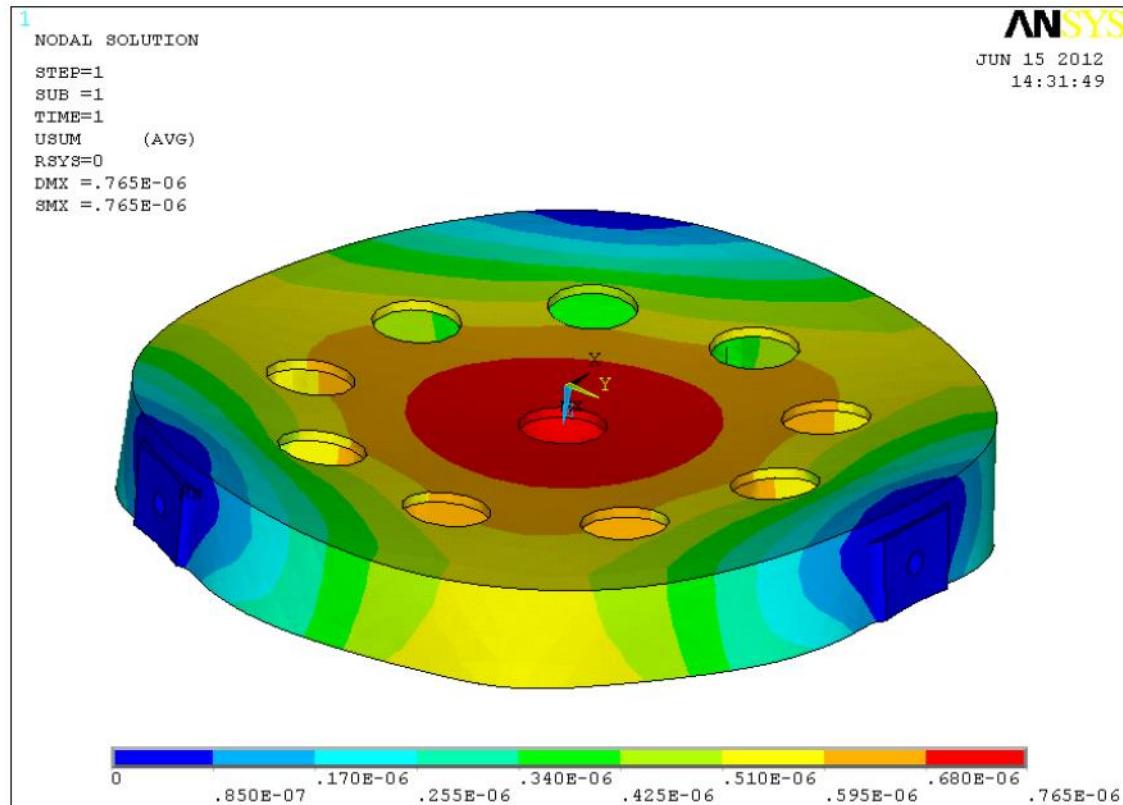


1 clamping area

First mode: 198 Hz

Tests by ADS Int.l

# Laboratory prototype - III



Static analysis (example)

30 g load

Deformation acceptable

Test requirements fulfilled

Design scalable to small / medium mission class

# Analysis of medium mission class payload

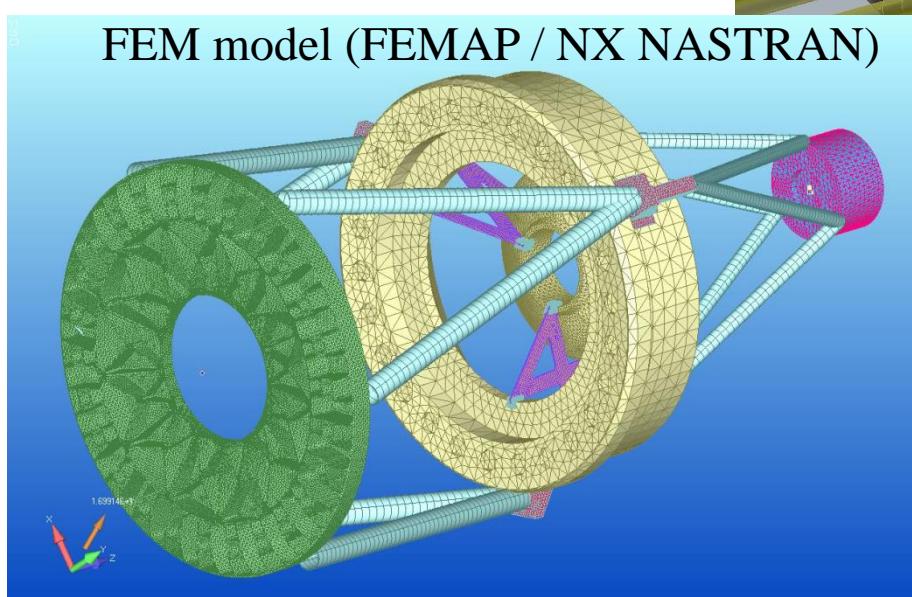
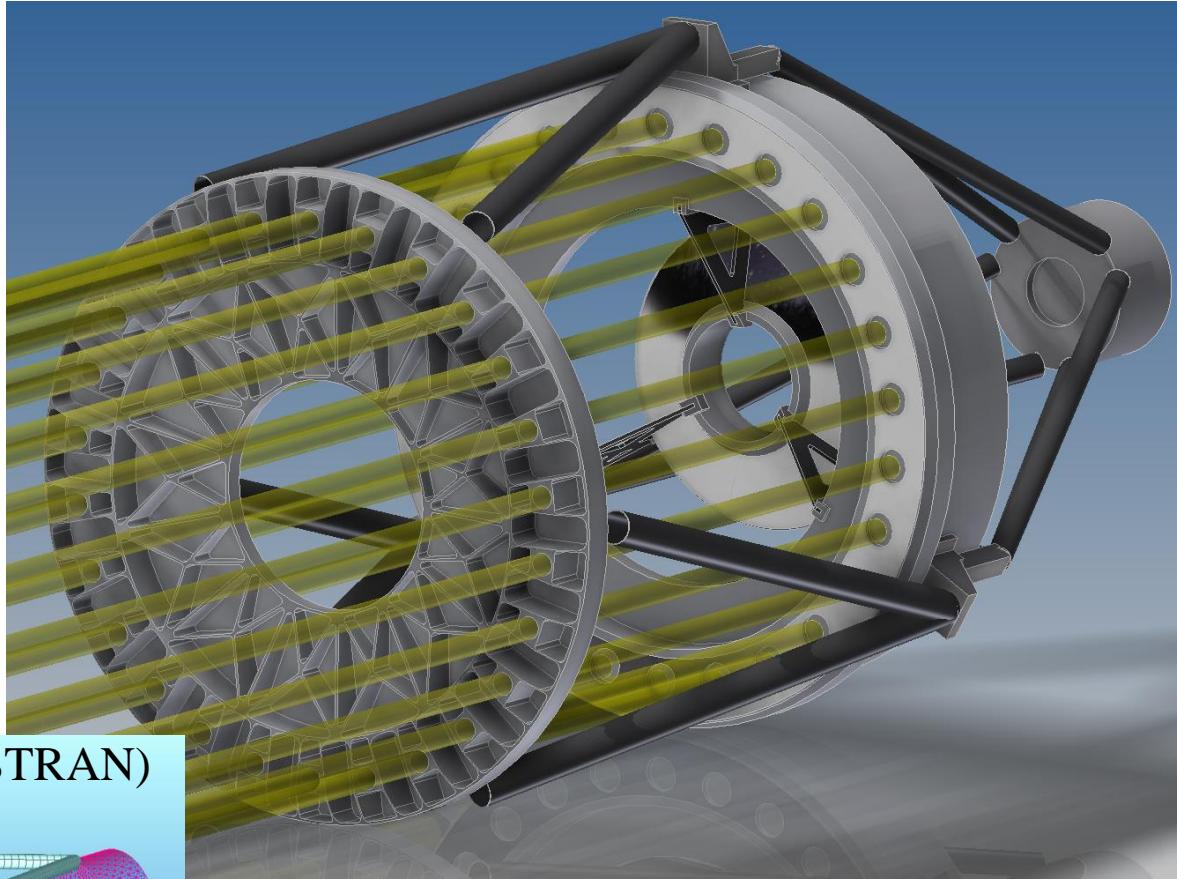
Telescope class: 1.5 m Ø

Trusses: CFRP

Optics: SiC

Invar clamps

FEM model (FEMAP / NX NASTRAN)



**Preliminary mass budget: 577 kg**

**Scaling to small mission: 72 kg**

Only pupil mask lightweighted

Additional lightweighting feasible

# Roadmap: from balloon (ISAS) to satellite (GAME)

## Gravitation Astrometric Measurement Experiment – GAME

Concept initially investigated for the satellite version

**Main goal:** Fundamental Physics (General Relativity tests);

**Secondary goal:** astrophysics by astrometry (solar system; exoplanets; ...)

### Current investigation: Precursor on stratospheric balloon

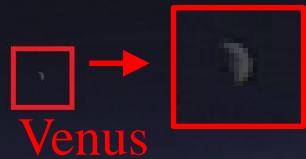
**Science goal:** astrometry of Solar System (major) planets

**Technical goal:** demonstration of main GAME concepts

## Interferometric Stratospheric Astrometry for Solar system - ISAS

**First technical launch:**

**Levaldigi airport, Dec. 9<sup>th</sup> 2013**



**Collaboration on stratospheric  
balloon experiments**

**INAF-OATo; ALTEC; Politecnico  
di Torino**

# Concluding remarks

- ✓ Astronomical techniques  $\Rightarrow$  Fundamental Physics
- ✓ GAME: PPN  $\gamma$  to  $10^{-7} - 10^{-8}$  range; PPN  $\beta$  to  $10^{-5} - 10^{-6}$  range
- ✓ Early development phase: flexible sub-system split

## Possible collaboration areas:

- Device and principle tests in lab and on sky
- Operations and data processing
- Selected sub-systems of payload and spacecraft
- Participation to data reduction and analysis consortium
- **High angular resolution Solar coronagraphy**

# GAME OVER

[PRESENTATION]

**Thanks to CAS and ESA!**